

QuickSort Algorithm

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Pseudocode:

```

QuickSort(A, low, high) {
  If (low < high) {
    Pivot = partition(A, low, high) //O(N)
    QuickSort(A, low, pivot-1) //T(k)
    QuickSort(A, pivot+1, high) //T(n-k)
  }
}
    
```

How it works?

8 2 7 1 11

Let's assume that 8 is our pivot. Then the array should be like this

2 7 1 8 11

1 2 7 8 11

1 2 7 8 11

$A[0 \dots 4]$

0 1 2 3 4
 8 11 1 7 2

Exchange will be based on this

0 1 2 3 4
 8 1 11 7 2

0 1 2 3 4
 8 1 7 11 2

0 1 2 3 4
 8 1 7 2 11

2 1 7 8 11

$X = A[0] = 8$ // partition = 8
 $i = 0$
 For \rightarrow from $j = 1$ to 4
 (When $j = 1$)
 If $(11 \leq 8) \rightarrow$ NO

 (When $j = 2$)
 If $(1 \leq 8) \rightarrow$ YES
 $i = 1$
 Exchange 11, 1

 (When $j = 3$)
 If $(7 \leq 8) \rightarrow$ YES
 $i = 2$
 Exchange 11, 7

 (When $j = 4$)
 If $(2 \leq 8) \rightarrow$ YES
 $i = 3$
 Exchange 2, 11

 Exchange 8, 2

Partition Method:

```

Algorithm
PARTITION(A, p, q) ▷ A[p..q]
1 x ← A[p] ▷ pivot = A[p]
2 i ← p
3 for j ← p+1 to q
4   do if A[j] ≤ x
5     then i ← i+1
6     exchange A[i] ↔ A[j]
7 exchange A[p] ↔ A[i]
8 return i
    
```

Recurrence Formula:

$$T(N) = T(k) + T(n-k) + O(n)$$

Here, k symbolizes the position of the pivot.

If pivot is in the middle $\rightarrow k = n/2$

$$\begin{aligned}
 T(N) &= T(n/2) + T(n-n/2) + O(n) \\
 &= T(n/2) + T(n/2) + O(n)
 \end{aligned}$$

This would have a time complexity $n \log_2(n) \rightarrow$ **BEST CASE**

QuickSort has **two types** of Time Complexity.
 If pivot is in the middle, then that is the best case.
 If pivot is in the start or end index, then that is the worst case.

QuickSort Worst Case