

# QuickSort Algorithm

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## Pseudocode:

```
QuickSort(A, low, high) {  
  if (low < high) {
```

Pivot = partition(A, low, high)	//O(N)
QuickSort(A, low, pivot-1)	//T(k)
QuickSort(A, pivot+1, high)	//T(n-k)

```
  }  
}
```

## How it works?

8	2	7	1	11
---	---	---	---	----

Let's assume that 8 is our pivot. Then the array should be like this

2	7	1	8	11
---	---	---	---	----

1	2	7	8	11
---	---	---	---	----

1	2	7	8	11
---	---	---	---	----

$A[0 \dots 4]$

0 1 2 3 4  
8 11 1 7 2

Exchange will be based on this

0 1 2 3 4  
8 1 11 7 2

0 1 2 3 4  
8 1 7 11 2

0 1 2 3 4  
8 1 7 2 11

2	1	7	8	11
---	---	---	---	----

$X = A[0] = 8$  // partition = 8

$i = 0$

For  $\rightarrow$  from  $j = 1$  to 4

(When  $j = 1$ )

If  $(11 \leq 8) \rightarrow$  NO

(When  $j = 2$ )

If  $(1 \leq 8) \rightarrow$  YES

$i = 1$

Exchange 11, 1

(When  $j = 3$ )

If  $(7 \leq 8) \rightarrow$  YES

$i = 2$

Exchange 11, 7

(When  $j = 4$ )

If  $(2 \leq 8) \rightarrow$  YES

$i = 3$

Exchange 2, 11

Exchange 8, 2

## Partition Method:

### Algorithm

$\text{PARTITION}(A, p, q) \triangleright A[p \dots q]$

1  $x \leftarrow A[p] \quad \triangleright \text{pivot} = A[p]$

2  $i \leftarrow p$

3 for  $j \leftarrow p+1$  to  $q$

4 do if  $A[j] \leq x$

5 then  $i \leftarrow i+1$

6 exchange  $A[i] \leftrightarrow A[j]$

7 exchange  $A[p] \leftrightarrow A[i]$

8 return  $i$

## Recurrence Formula:

$$T(N) = T(k) + T(n-k) + O(n)$$

Here,  $k$  symbolizes the position of the pivot.

If pivot is in the middle  $\rightarrow k = n/2$

$$T(N) = T(n/2) + T(n-n/2) + O(n)$$

$$= T(n/2) + T(n/2) + O(n)$$

This would have a time complexity  $\log_2(n) \rightarrow$  **BEST CASE**

QuickSort has **two types** of Time Complexity.

If pivot is in the middle, then that is the best case.

If pivot is in the start or end index, then that is the worst case.

## QuickSort Worst Case